## Progression of Skills and Knowledge - Maths



## Nursery

Children will be learning to:

- Develop fast recognition of up to 3 objects, without having to count them individually ('subitising'). Recite numbers past 5. Say one number for each item in order: 1,2,3,4,5.
- Know that the last number reached when counting a small set of objects tells you how many there are in total ('cardinal principle').
- Show 'finger numbers' up to 5 .
- Link numerals and amounts: for example, showing the right number of objects to match the numeral, up to 5 .
- Experiment with their own symbols and marks as well as numerals.
- Solve real world mathematical problems with numbers up to 5.
- Compare quantities using language: 'more than', 'fewer than'.
- Talk about and explore 2D and 3D shapes (for example, circles, rectangles, triangles and cuboids) using informal and mathematical language: 'sides', 'corners'; 'straight', 'flat', 'round'.
- Understand position through words alone - for example, "The bag is under the table," - with no pointing.
- Describe a familiar route.
- Discuss routes and locations, using words like 'in front of' and 'behind'.


## EYFS Maths:

## Reception

Children will be learning to:

- Count objects, actions and sounds.
- Subitise
- Link the number symbol (numeral) with its cardinal number value.
- Count beyond 10.
- Compare numbers.
- Understand the 'one more than/ one less than' relationship between consecutive numbers.
- Explore the composition of numbers to 10.
- Automatically recall number bonds for numbers 0 to 5 and some to 10 .
- Select, rotate and manipulate shapes to develop spatial reasoning skills.
- Compose and decompose shapes so that children recognise a shape can have other shapes within it, just as numbers can
- Continue, copy and create repeating patterns
- Compare length, weight and capacity


## Early Learning Goals

Number

- Have a deep understanding of number to 10 , including the composition of each number.
- Subitise (recognise quantities without counting) up to 5 .
- Make comparisons between objects relating to size, length, weight and capacity.
- Select shapes appropriately: flat surfaces for building, a triangular prism for a roof, etc.
- Combine shapes to make new ones - an arch, a bigger triangle, etc.
- Talk about and identify the patterns around them. For example: stripes on clothes, designs on rugs and wallpaper.
- Use informal language like 'pointy', 'spotty', 'blobs', etc.
- Extend and create $A B A B$ patterns - stick, leaf, stick, leaf.
- Notice and correct an error in a repeating pattern.
- Begin to describe a sequence of events, real or fictional, using words such as 'first', 'then...'
- Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10 , including double facts.


## Numerical Patterns

- Verbally count beyond 20 , recognising the pattern of the counting system.
- Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity.
- Explore and represent patterns within numbers up to 10 , including evens and odds, double facts and how quantities can be distributed equally.

| Year 1-3 Maths: |  |  |  |
| :---: | :---: | :---: | :---: |
| Topic | Year 1 | Year 2 | Year 3 |
| Place Value | - count to and across 100, forwards and backwards, beginning with 0 or 1 , or from any given number <br> - count, read and write numbers to 100 in numerals; count in multiples of $2 \mathrm{~s}, 5 \mathrm{~s}$ and 10 s <br> - given a number, identify 1 more and 1 less <br> - identify and represent numbers using objects and pictorial representations including the number line, and use the language of: equal to, more than, less than (fewer), most, least <br> - read and write numbers from 1 to 20 in numerals and words | - count in steps of 2,3 , and 5 from 0 , and in 10 s from any number, forward and backward <br> - recognise the place value of each digit in a two-digit number (10s and 1s) <br> - identify, represent and estimate numbers using <br> - different representations, including the number <br> - line <br> - compare and order numbers from 0 up to 100; <br> - use <, > and = signs <br> - read and write numbers to at least 100 in <br> - numerals and in words <br> - use place value and number facts to solve problems | - count from 0 in multiples of $4,8,50$ and 100; find 10 or 100 more or less than a given number <br> - recognise the place value of each digit in a 3 - digit number (100s, 10s, 1s) <br> - compare and order numbers up to 1,000 <br> - identify, represent and estimate numbers <br> - using different representations <br> - read and write numbers up to 1,000 in numerals and in words <br> - solve number problems and practical problems involving these ideas |
| Addition and Subtraction | - read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs <br> - represent and use number bonds and related subtraction facts within 20 <br> - add and subtract one-digit and twodigit numbers to 20 , including 0 <br> - solve one-step problems that involve addition and subtraction, using concrete objects and pictorial | - solve problems with addition and subtraction: <br> - using concrete objects and pictorial representations, including those involving numbers, quantities and measures <br> - applying their increasing knowledge of mental and written methods <br> - recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 <br> - add and subtract numbers using concrete objects, pictorial | - add and subtract numbers mentally, including: <br> - a three-digit number and 1 s <br> - a three-digit number and 10s <br> - a three-digit number and 100 s <br> - add and subtract numbers with up to 3 digits, using formal written methods of columnar addition and subtraction <br> - estimate the answer to a calculation and use inverse operations to check answers <br> - solve problems, including missing number problems, using number |


|  | representations, and missing number problems such as $7=$ ? - 9 | representations, and mentally, including: <br> - a two-digit number and 1 s <br> - a two-digit number and 10 s <br> - 2 two-digit numbers <br> - adding 3 one-digit numbers <br> - show that addition of 2 numbers can be done in any order (commutative) and subtraction of 1 number from another cannot <br> - recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems | facts, place value, and more complex addition and subtraction |
| :---: | :---: | :---: | :---: |
| Multiplication and Division | - solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher | - recall and use multiplication and division facts for the 2,5 and 10 multiplication tables, including recognising odd and even numbers <br> - calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication $(\times)$, division ( $\div$ ) and equals ( $=$ ) signs <br> - show that multiplication of 2 numbers can be done in any order (commutative) and division of 1 number by another cannot <br> - solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts | - recall and use multiplication and division facts for the 3,4 and 8 multiplication tables <br> - write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods <br> - solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which $n$ objects are connected to m objects |


| Fractions | - recognise, find and name a half as 1 of 2 equal parts of an object, shape or quantity <br> - recognise, find and name a quarter as 1 of 4 equal parts of an object, shape or quantity | - recognise, find, name and write fractions $\frac{1}{3}, \frac{1}{4}, \frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity <br> - write simple fractions, for example $\frac{1}{2}$ of $6=3$ and recognise the equivalence of $\frac{2}{4}$ and $\frac{1}{2}$ | - count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 <br> - recognise, find and write fractions of a discrete set of objects: unit fractions and non- unit fractions with small denominators <br> - recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators <br> - recognise and show, using diagrams, equivalent fractions with small denominators <br> - add and subtract fractions with the same denominator within one whole [for example $\frac{5}{7}, \frac{1}{7}$ and $\frac{6}{7}$ ] <br> - compare and order unit fractions, and fractions with the same denominators <br> - solve problems that involve all of the above |
| :---: | :---: | :---: | :---: |
| Measurement | - compare, describe and solve practical problems for: <br> - lengths and heights [for example, long/short, longer/shorter, tall/short, double/half] <br> - mass/weight [for example, heavy/light, heavier than, lighter than] <br> - capacity and volume [for example, full/empty, more than, less than, half, half full, quarter] | - choose and use appropriate standard units to estimate and measure length/height in any direction ( $\mathrm{m} / \mathrm{cm}$ ); mass (kg/g); temperature $\left({ }^{\circ} \mathrm{C}\right.$ ); capacity (litres $/ \mathrm{ml}$ ) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels <br> - compare and order lengths, mass, volume/capacity and record the results using >, < and = | - measure, compare, add and subtract: lengths ( $\mathrm{m} / \mathrm{cm} / \mathrm{mm}$ ); mass ( $\mathrm{kg} / \mathrm{g}$ ); volume/capacity ( $1 / \mathrm{ml}$ ) <br> - measure the perimeter of simple 2-D shapes <br> - add and subtract amounts of money to give <br> - change, using both $£$ and $p$ in practical <br> - contexts <br> - tell and write the time from an analogue |


|  | - time [for example, quicker, slower, earlier, later] <br> - measure and begin to record the following: <br> - lengths and heights <br> - mass/weight <br> - capacity and volume <br> - time (hours, minutes, seconds) <br> - recognise and know the value of different denominations of coins and notes <br> - sequence events in chronological order using language [for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] <br> - recognise and use language relating to dates, including days of the week, weeks, months and years <br> - tell the time to the hour and half past the hour and draw the hands on a clock face to show these times |
| :---: | :---: |
| $\begin{aligned} & \text { Geometry - } \\ & \text { Properties of Shape } \end{aligned}$ | - describe position, direction and movement, including whole, half, quarter and three- quarter turns |

- recognise and use symbols for pounds ( f ) and pence ( p ); combine amounts to make a particular value
- find different combinations of coins that equal the same amounts of money
- solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change
- compare and sequence intervals of time tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times
- know the number of minutes in an hour and the number of hours in a day
- identify and describe the properties of 2-D shapes, including the number of sides, and line symmetry in a vertical line
- identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces
- identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid]
- compare and sort common 2-D and $3-\mathrm{D}$ shapes and everyday objects
- clock, including using Roman numerals from 1
- to XII, and 12-hour and 24-hour clocks
- estimate and read time with increasing
- accuracy to the nearest minute; record and compare time in terms of seconds, minutes and hours; use vocabulary such as o'clock, am/pm, morning, afternoon, noon and midnight
- know the number of seconds in a minute and the number of days in each month, year and leap year
- compare durations of events [for example, to
- calculate the time taken by particular events or tasks]
- draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them
- recognise angles as a property of shape or a description of a turn
- identify right angles, recognise that 2
- right angles make a half-turn, 3 make three-quarters of a turn and 4 a complete turn; identify whether angles are greater than or less than a right angle

|  |  |  | - identify horizontal and vertical lines and pairs of perpendicular and parallel lines |
| :---: | :---: | :---: | :---: |
| Geometry - Position and Direction | - describe position, direction and movement, including whole, half, quarter and three- quarter turns | - order and arrange combinations of mathematical objects in patterns and sequences <br> - use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise) |  |
| Statistics |  | - interpret and construct simple pictograms, tally charts, block diagrams and tables <br> - ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity <br> - ask-and-answer questions about totalling and comparing categorical data | - interpret and present data using bar charts, pictograms and tables <br> - solve one-step and two-step questions [for example 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables |


| Year 4-6 Maths: |  |  |  |
| :---: | :---: | :---: | :---: |
| Topic | Year 4 | Year 5 | Year 6 |
| Place Value | - count in multiples of 6, 7, 9, 25 and 1,000 <br> - find 1,000 more or less than a given number <br> - count backwards through 0 to include negative numbers <br> - recognise the place value of each digit in a four-digit number ( 1,000 s, $100 \mathrm{~s}, 10 \mathrm{~s}$, and 1 s ) <br> - order and compare numbers beyond 1,000 <br> - identify, represent and estimate numbers <br> - using different representations <br> - round any number to the nearest 10 , 100 or 1,000 <br> - solve number and practical problems that involve all of the above and with increasingly large positive numbers <br> - read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of 0 and place value | - read, write, order and compare numbers to at least 1,000,000 and determine the value of each digit <br> - count forwards or backwards in steps of powers of 10 for any given number up to 1,000,000 <br> - interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through 0 <br> - round any number up to $1,000,000$ to the nearest $10,100,1,000,10,000$ and 100,000 <br> - solve number problems and practical problems that involve all of the above <br> - read Roman numerals to 1,000 (M) and recognise years written in Roman numerals | - read, write, order and compare numbers up to $10,000,000$ and determine the value of each digit <br> - round any whole number to a required degree of accuracy <br> - use negative numbers in context, and calculate intervals across 0 <br> - solve number and practical problems that involve all of the above |


| Addition and Subtraction | - add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate <br> - estimate and use inverse operations to check answers to a calculation - solve addition and subtraction twostep <br> - problems in contexts, deciding which operations and methods to use and why | - add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) <br> - add and subtract numbers mentally with increasingly large numbers - use rounding to check answers to calculations and <br> - determine, in the context of a problem, levels of accuracy <br> - solve addition and subtraction multistep problems in contexts, deciding which operations and methods to use and why | - perform mental calculations, including with mixed operations and large numbers <br> - use their knowledge of the order of operations to carry out calculations involving the 4 operations <br> - solve addition and subtraction multistep problems in contexts, deciding which operations and methods to use and why <br> - solve problems involving addition, subtraction, multiplication and division <br> - use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy |
| :---: | :---: | :---: | :---: |
| Multiplication and Division | - recall multiplication and division facts for multiplication tables up to $12 \times 12$ <br> - use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together 3 numbers <br> - recognise and use factor pairs and commutativity in mental calculations <br> - multiply two-digit and three-digit numbers by a one-digit number using formal written layout <br> - solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder | - identify multiples and factors, including finding all factor pairs of a number, and common factors of 2 numbers <br> - know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers <br> - establish whether a number up to 100 is prime and recall prime numbers up to 19 <br> - multiply numbers up to 4 digits by a one- or two- digit number using a formal written method, including long multiplication for two-digit numbers <br> - multiply and divide numbers mentally, drawing upon known facts <br> - divide numbers up to 4 digits by a one-digit number using the formal | - multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication <br> - divide numbers up to 4 digits by a two- digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context <br> - divide numbers up to 4 digits by a two- digit number using the formal written method of short division where appropriate, interpreting remainders according to the context |


|  | correspondence problems such as n objects are connected to mobjects | written method of short division and interpret remainders appropriately for the context <br> - multiply and divide whole numbers and those involving decimals by 10 , 100 and 1,000 <br> - recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3) <br> - solve problems involving multiplication and division, including using their knowledge of factors and multiples, squares and cubes <br> - solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign <br> - solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates | - identify common factors, common multiples and prime numbers |
| :---: | :---: | :---: | :---: |
| Fractions (including decimals and percentages Year 5/6) | - recognise and show, using diagrams, families of common equivalent fractions <br> - count up and down in hundredths; recognise that hundredths arise when dividing an object by 100 and dividing tenths by 10 <br> - solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | - compare and order fractions whose denominators are all multiples of the same number <br> - identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths <br> - recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number <br> - [for example, $\frac{2}{5}+\frac{4}{5}=\frac{6}{5}=1 \frac{1}{5}$ ] | - use common factors to simplify fractions; use common multiples to express fractions in the same denomination <br> - compare and order fractions, including fractions >1 <br> - add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions <br> - multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $1 / 4 \times 1 / 2=$ 1/8] |

- add and subtract fractions with the same denominator
- recognise and write decima equivalents of any number of tenths or hundreds
- recognise and write decimal equivalents to $1 / 4,1 / 2$ and $3 / 4$.
- find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths
- round decimals with 1 decimal place to the nearest whole number
- compare numbers with the same number of decimal places up to 2 decimal places
- solve simple measure and money problems involving fractions and decimals to 2 decimal places

Measurement

- add and subtract fractions with the same denominator, and denominators that are multiples of the same number
- multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams
- read and write decimal numbers as fractions [for example, $0.71=\frac{71}{100}$ ]
- recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents
- round decimals with 2 decimal places to the nearest whole number and to 1 decimal place
- read, write, order and compare numbers with up to 3 decimal places
- solve problems involving number up to 3 decimal places
- recognise the per cent symbol (\%) and understand that per cent relates to 'number of parts per 100', and write percentages as a fraction with denominator 100, and as a decimal fraction
solve problems which require knowing percentage and decimal

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$$ equivalents of $\overline{2}, \overline{4}, \overline{5}, \frac{2}{5}, \overline{5}$ and those fractions with a denominator of a multiple of 10 or 25

- convert between different units of metric measure [for example, kilometre and metre; centimetre and
- divide proper fractions by whole numbers [for example, $\frac{1}{3} \div 2=\frac{1}{6}$ ]
- associate a fraction with division and
- calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 3/8]
- identify the value of each digit in numbers given to 3 decimal places and multiply and divide numbers by 10,100 and 1,000 giving answers up to 3 decimal places
- multiply one-digit numbers with up to 2 decimal places by whole numbers
- use written division methods in cases where the answer has up to 2 decimal places
- solve problems which require answers to be rounded to specified degrees of accuracy
- recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
- solve problems involving the calculation and conversion of units of measure, using decimal notation up

|  | - measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres <br> - find the area of rectilinear shapes by counting squares <br> - estimate, compare and calculate different measures, including money in pounds and pence <br> - read, write and convert time between analogue and digital 12and 24 -hour clocks <br> - solve problems involving converting from hours to minutes, minutes to seconds, years to months, weeks to days | metre; centimetre and millimetre; gram and kilogram; litre and millilitre] <br> - understand and use approximate equivalences between metric units and common imperial units such as inches, pounds and pints <br> - measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres <br> - calculate and compare the area of rectangles (including squares), including using standard units, square centimetres (cm2) and square metres (m2), and estimate the area of irregular shapes <br> - estimate volume [for example, using 1 cm 3 blocks to build cuboids (including cubes)] and capacity [for example, using water] <br> - solve problems involving converting between units of time <br> - use all four operations to solve problems involving measure [for example, length, mass, volume, money] using decimal notation, including scaling | to 3 decimal places where appropriate <br> - use, read, write and convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to up to 3 decimal places <br> - convert between miles and kilometres <br> - recognise that shapes with the same areas can have different perimeters and vice versa <br> - recognise when it is possible to use formulae for area and volume of shapes <br> - calculate the area of parallelograms and triangles <br> - calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm3) and cubic metres (m3), and extending to other units [for example, mm3 and km3] |
| :---: | :---: | :---: | :---: |
| Geometry Properties of Shape | - compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes <br> - identify acute and obtuse angles and compare and order angles up to 2 right angles by size | - identify 3-D shapes, including cubes and other cuboids, from 2-D representations <br> - know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles <br> - draw given angles, and measure them in degrees ( ${ }^{\circ}$ ) <br> - identify: | - draw 2-D shapes using given dimensions and angles <br> - recognise, describe and build simple 3-D shapes, including making nets <br> - compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons |


|  | - identify lines of symmetry in 2-D shapes presented in different orientations <br> - complete a simple symmetric figure with respect to a specific line of symmetry | - angles at a point and 1 whole turn (total $360^{\circ}$ ) <br> - angles at a point on a straight line and half a turn (total $180^{\circ}$ ) <br> - other multiples of $90^{\circ}$ <br> - use the properties of rectangles to deduce related facts and find missing lengths and angles <br> - distinguish between regular and irregular polygons based on reasoning about equal sides and angles | - illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius <br> - recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles |
| :---: | :---: | :---: | :---: |
| Geometry - Position and Direction | - describe positions on a 2-D grid as coordinates in the first quadrant <br> - describe movements between positions as translations of a given unit to the left/right and up/down <br> - plot specified points and draw sides to complete a given polygon | - identify, describe and represent the position of a shape following a reflection or translation, using the appropriate language, and know that the shape has not changed | - describe positions on the full coordinate grid (all 4 quadrants) <br> - draw and translate simple shapes on the coordinate plane, and reflect them in the axes |
| Statistics | - interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs <br> - solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs | - solve comparison, sum and difference problems using information presented in a line graph <br> - complete, read and interpret information in tables, including timetables | - interpret and construct pie charts and line graphs and use these to solve problems <br> - calculate and interpret the mean as an average |
| Ratio and Proportion |  |  | - solve problems involving the relative sizes of 2 quantities where missing values can be found by using integer multiplication and division facts <br> - solve problems involving the calculation of percentages [for example, of measures and such as $15 \%$ of 360 ] and the use of percentages for comparison |


|  |  |  | - solve problems involving similar shapes where the scale factor is known or can be found <br> - solve problems involving unequal sharing and grouping using knowledge of fractions and multiples |
| :---: | :---: | :---: | :---: |
| Algebra |  |  | - use simple formulae <br> - generate and describe linear number sequences <br> - express missing number problems algebraically <br> - find pairs of numbers that satisfy an equation with 2 unknowns <br> - enumerate possibilities of combinations of 2 variables |

